## KULEUVEN

# Masking Lattice-based Post-quantum Cryptography 

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## Side-channel attacks (SCA) exploits implementation flaws

- Power consumption
- Electromagnetic radiation
- Timing information


Leak sensitive information

## Masking is a countermeasure of SCA



## Higher-order (t-order) masking can prevent higher-order (t-order) SCA

- t-order masking:
- Sensitive value splits into (t+1) shares
- Perform all operations on each share separately

- Attack model:
- Adversary can see up to $t$ intermediate sensitive values


## Arithmetic masking used for arithmetic operations



Useful for arithmetic operations:

- modular addition,
- modular subtraction,
- modular multiplication


## Boolean masking used for bitwise operations



Useful for Boolean operations:

- xor
- and
- or
- shift


## Goals

- Side-channel secure post-quantum MLWE/MLWR based KEM
- Saber: MLWR based KEM (3rd round finalist)

$$
\lfloor A \cdot \mathbf{s}\rceil=\mathbf{b} \quad \text { and } \quad \mathbf{b}^{\prime} \text { random }
$$

$\mathbf{b}^{\prime}$ and $\mathbf{b}$ indistinguishable

- Generalized masked implementation
- Parameterized security order


## Challenges

- MLWE/MLWR based constructions uses arithmetic and Boolean operations
- Conversion algorithms are expensive
- Masked polynomial comparison
- Easy for first-order
- Costly for higher-order


## Saber is a Key-encapsulation mechanism

- Based on module learning with rounding (MLWR) problem $\quad\lfloor A \cdot \mathbf{s}\rceil=\mathbf{b}$
- Variant of learning with errors (LWE) problem $A \cdot \mathbf{s}+\mathbf{e}=\mathbf{b}$
- NIST 3rd-round finalist
- Algorithms: Key-Generation, Encapsulation, and Decapsulation
- CCA secure KEM
- Same secret-key used for multiple Decapsulation


## Decapsulation is SCA sensitive operation of Saber



Decapsulation algorithm of Saber

## Arithmetic masked operations of Saber is represented with color blue



Decapsulation algorithm of Saber
Arithmetic masking

## Addition and multiplication operations are duplicates for each shares

## Addition

- $z=x+y$
- $\mathrm{x}=\mathrm{x}_{0}+\mathrm{x}_{1}+\ldots+\mathrm{x}_{\mathrm{t}}$
- When $y$ is not masked
- $z_{0}=x_{0}+y$
- $z_{i}=x_{i} \quad \forall i=1, \ldots, t$
- $z=z_{0}+z_{1}+\ldots+z_{t}$


## Addition and multiplication operations are duplicates for each shares

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- When $y$ is masked
- $y=y_{0}+y_{1}+\ldots+y_{t}$
- $z_{i}=x_{i}+y_{i} \forall i=0, \ldots, t$
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## Addition

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- When y is masked
- $y=y_{0}+y_{1}+\ldots+y_{t}$
- $z_{i}=x_{i}+y_{i} \forall i=0, \ldots, t$
- $z=z_{0}+z_{1}+\ldots+z_{t}$

Multiplication

- $z=x . y$
- Only one polynomial masked (x)
- $\mathrm{x}=\mathrm{x}_{0}+\mathrm{x}_{1}+\ldots+\mathrm{x}_{\mathrm{t}}$
- $z_{i}=x_{i} \cdot y \quad \forall i=0, \ldots, t$
- $z=z_{0}+z_{1}+\ldots+z_{t}$


## Boolean masked operations of Saber is represented with color Orange



## Masked Centered Binomial Distribution $(\beta \mu)$ use both making techniques

- Uses Boolean to Arithmetic conversion (B2A)
- B2A is one of the costly operations


Arithmetic masking
Boolean masking
Both masking

## A2B is needed to convert arithmetic shares to Boolean shares

- Before shift we use arithmetic to Boolean conversion (A2B)
- A2B is another costly operation


Arithmetic masking
Boolean masking
Both masking
A2B conversion

## Implementation results of masked Saber are in the table

| Saber Decapsulation | Unmasked | 1st-order | 2nd-order | 3rd-order |
| :---: | :---: | :---: | :---: | :---: |
| Performance <br> $[\mathrm{k}] C P U$ cycles | 1,121 | $3,022(2.69 \mathrm{x})$ | $5,567(4.96 \mathrm{x})$ | $8,649(7.71 \mathrm{x})$ |
| Random bytes | 0 | 12 k | 42 k | 91 k |

Platform: ARM Cortex-M4

Framework: PQM4 [1]
Compiled with: arm-none-eabi-gcc
Version: 9.2.1 Schwabe, P., Stoffelen, K., https://github.com/mupg/pgm4.

## Masked Saber perform better than masked Kyber


[1] Bitslicing arithmetic/boolean masking conversions for fun and profit with application to lattice-based kems, Bronchain, O., Cassiers, G., https://eprint.iacr.org/2022/158.

## Masked uSaber perform even better than masked Saber



| uSaber | Ours |
| :---: | :---: |
| Saber | Ours |
| Kyber | $[1]$ |

## Performance (x1000 cpucycle)

## Decapsulation operation of Kyber is similar to Saber



Decapsulation algorithm of Kyber

## A2B conversion algorithm [1]

Input : $\left\{x_{i}\right\}_{0 \leq i \leq t}$ such that $x=\sum x_{i} \bmod 2^{k}$
Output : $\left\{\mathrm{c}_{\mathrm{i}}\right\}_{0 \leq i \leq t}$ such that $\oplus \mathrm{C}_{\mathrm{i}}=\sum \mathrm{x}_{\mathrm{i}} \bmod 2^{\mathrm{k}}$

1. $\left\{y_{i}\right\}_{0 \leq i \leq t / 2} \leftarrow A 2 B\left(\left\{x_{i}\right\}_{0 \leq i s t / 2}\right)$
2. $\left\{y_{i}\right\}_{0 \leq i s t} \leftarrow$ Expand $\left(\left\{y_{i}\right\}_{0 \leq i s t / 2}\right)$
3. $\left.\left\{z_{i}\right\}_{0 \leq i s t / 2} \leftarrow \mathrm{~A} 2 \mathrm{~B}\left(\left\{\mathrm{x}_{\mathrm{i}}\right\}_{(\mathrm{t} / 2}+1\right) \leq \mathrm{sist/2}\right)$
4. $\left\{z_{\mathrm{i}}\right\}_{0 \leq i s t} \leftarrow$ Expand $\left(\left\{z_{\mathrm{i}}\right\}_{0 \leq i s t / 2}\right)$
5. $\left\{\mathrm{c}_{\mathrm{i}}\right\}_{0 \leq i \leq t} \leftarrow \operatorname{Sec} A d d\left(\left\{y_{i}\right\}_{0 \leq i \leq t},\left\{z_{i}\right\}_{0 \leq i s t}\right)$
6. return $\left\{c_{i}\right\}_{0 \leq i s t}$
[1] Tobias Schneider, Clara Paglialonga, Tobias Oder, and Tim Güneysu. Efficiently masking binomial sampling at arbitrary orders for lattice based crypto. In Dongdai Lin and Kazue Sako, editors, PKC 2019, Part II, volume 11443 of LNCS, pages 534-564. Springer, Heidelberg, April 2019.

## Steps of A2B conversion algorithm

Input : $\left\{x_{\mathrm{i}}\right\}_{0 \leq i \leq 3}$ such that $\mathrm{x}=\sum \mathrm{x}_{\mathrm{i}} \bmod 2^{\mathrm{k}}$
Output: $\left\{c_{i}\right\}_{0 \leq i \leq 3}$ such that $\oplus c_{i}=\sum x_{i}$

| Input | $\mathrm{x}_{0}$ | $\mathrm{x}_{1}$ | $\mathrm{x}_{2}$ |
| :--- | :--- | :--- | :--- |


| $\mathrm{c}_{0}$ | $\mathrm{c}_{1}$ | $\mathrm{c}_{2}$ | $\mathrm{c}_{3}$ |
| :--- | :--- | :--- | :--- |$\quad{ }_{\mathrm{C}} \mathrm{C}_{\mathrm{i}}=\sum \mathrm{x}_{\mathrm{i}}$

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## Steps of A2B conversion algorithm

Input : $\left\{\mathrm{x}_{\mathrm{i}}\right\}_{0 \leq \leq \leq 3}$ such that $\mathrm{x}=\sum \mathrm{x}_{\mathrm{i}} \bmod 2^{\mathrm{k}}$
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Output

$$
\begin{array}{l|l|l|l|}
\mathrm{c}_{0} & \mathrm{c}_{1} & \mathrm{c}_{2} & \mathrm{c}_{3} \\
\hline
\end{array} \quad \oplus \mathrm{c}_{\mathrm{i}}=\sum \mathrm{x}_{\mathrm{i}}
$$

Expand

$$
\begin{aligned}
& x_{0}=y_{0}^{\prime} \oplus y_{1}^{\prime} \\
& x_{1}=z_{0}^{\prime} \oplus z_{1}^{\prime}
\end{aligned}
$$

SecAdd
$\left(x_{0}+x_{1}\right) \bmod 2^{k}=$
$\left(y_{0}^{\prime} \oplus \quad y^{\prime}{ }_{1}\right)+\left(z_{0}^{\prime} \oplus \quad z^{\prime}{ }_{1}\right)$
$\bmod 2^{k}$

$$
\begin{array}{|l|l|}
\hline \mathrm{c}_{0}^{\prime} & \mathrm{c}_{1}^{\prime} \\
\hline
\end{array} \quad=\quad \mathrm{c}_{0}^{\prime} \quad \oplus \quad \mathrm{c}_{1}^{\prime}
$$

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$\bmod 2^{k}$

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SecAdd
$\left(x_{0}+x_{1}\right) \bmod 2^{k}=$
$\left(y_{0}^{\prime} \oplus \quad y^{\prime}{ }_{1}\right)+\left(z_{0}^{\prime} \oplus \quad z^{\prime}{ }_{1}\right)$
$\bmod 2^{k}$

## Compression operation in Saber is just shift operation

Input : $\left\{x_{i}\right\}_{0 \leq i \leq t}$ such that $x=\sum x_{i} \bmod 2^{k}$
Output: $\left\{m_{i}\right\}_{0 \leq i \leq t}$ such that $\oplus m_{i}=\operatorname{MSB}\left(\sum x_{i} \bmod 2^{k}\right)$

1. $\left\{c_{i}\right\}_{0 \leq i s t} \leftarrow A 2 B\left(\left\{x_{i}\right\}_{0 \leq i s t}\right)$
2. $\left\{m_{i}\right\}_{0 \leq i s t} \leftarrow \operatorname{MSB}\left(\left\{c_{i}\right\}_{0 \leq i s t / 2}\right)$
3. return $\left\{m_{i}\right\}_{0 \leq i s t}$

## Compression operation in Kyber has lot more steps than Saber

Input : $\left\{\mathrm{x}_{\mathrm{i}}\right\}_{0 \leq i \leq t}$ such that $\mathrm{x}=\sum \mathrm{x}_{\mathrm{i}} \bmod \mathrm{q}$
Output: $\left\{m_{i}\right\}_{0 \leq i s t}$ such that $\oplus m_{i}=$ Compression $\left(\sum x_{i} \operatorname{modq}\right)$

1. $x_{0} \leftarrow x_{0}-\lfloor q / 4\rfloor$
2. $\left\{y_{i}\right\}_{0 \leq i \leq t} \leftarrow$ transform-power-of-2 $\left(\left\{x_{i}\right\}_{0 \leq i \leq t t^{\prime}} 13\right)$
3. $\mathrm{y}_{0} \leftarrow \mathrm{y}_{0}-\lfloor\mathrm{q} / 2\rfloor$
4. $\left\{\mathrm{c}_{\mathrm{i}}\right\}_{0 \leq i \leq \mathrm{t}} \leftarrow \mathrm{A} 2 \mathrm{~B}\left(\left\{\mathrm{y}_{\mathrm{i}}\right\}_{0 \leq i \leq \mathrm{t}}\right)$
5. $\left\{m_{i}\right\}_{0 \leq i s t} \leftarrow M S B\left(\left\{c_{i}\right\}_{0 \leq i s t / 2}\right)$
6. return $\left\{m_{i}\right\}_{0 \leq i \leq t}$

## Future works

- Masking friendly post-quantum schemes
- Improve the performances of masking building block
- Reduce random bytes requirements in masked scheme


## Publication:

Suparna Kundu, Jan-Pieter D'Anvers, Michiel Van Beirendonck, Angshuman Karmakar, Ingrid Verbauwhede "Higher-order masked Saber". SCN 2022.

## Thank you!

